

# Dimensions in the Object Oriented Software Development Process

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## Abstract

*During the object-oriented software development process, a variety of models of the system is built. All these models are not independent, but they are related to each other. Elements in one model have trace dependencies to other models; they are semantically overlapping and together represent the system as a whole.*

*It is necessary to have a precise definition of the syntax and semantics of the different models and their relationships, since the lack of accuracy in their definition can lead to wrong model interpretations and inconsistency between models.*

*In this paper we classify relationships between models along three different dimensions, proposing a formal description of them. The goal of the proposed formalization is to provide formal foundations for tools that perform intelligent analysis on models assisting software engineers through the development process.*

**Keywords:** software development process, modeling notations, formal methods, relations between models, case tools.

## 1. Introduction

A software development process, e.g. The Unified Process (Jacobson et al., 1999), Catalysis (D'Souza and Wills, 1998), Fusion (Coleman et al. 1994) is a set of activities needed to transform user's requirements into a software system. Modern software development processes are iterative and incremental, they repeat over a series of iterations making up the life cycle of a system. Each iteration takes place over time and it consists of one pass through the requirements, analysis, design, implementation and test activities, building a number of different artifacts (i.e models). All these artifacts are not independent; they are related to each other, they are semantically overlapping and together represent the system as a whole. Elements in one artifact have trace dependencies to other artifacts. For instance, a use case (in the use-case

model) can be traced to a collaboration (in the design model) representing its realization.

On the other hand, due to the incremental nature of the process, each iteration results in an increment of artifacts built in previous iterations. An increment is not necessarily additive. Generally in the early phases of the life cycle, a superficial model is replaced with a more detailed or sophisticated one, but in later phases increments are typically additive, i.e. a model is enriched with new features, while previous features are preserved.

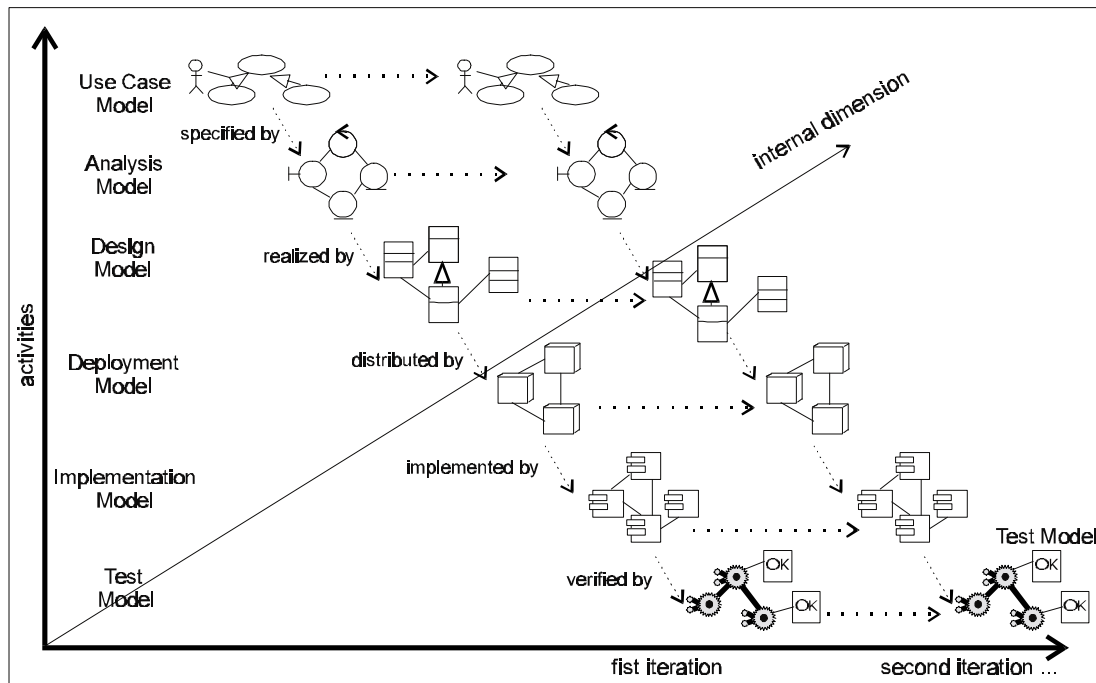
Different relationships existing between models can be organized along the following three dimensions:

- internal dimension (artifact dimension )
- vertical dimension (activity dimension )
- horizontal dimension (iteration dimension )

The **internal** dimension deals with relations between sub-models that coexists consistently making up a more complex model. For instance, an analysis model consists of analysis class diagram, interaction diagrams, collaboration diagrams. All the artifacts within a single model are related and have to be compatible with each other.

The **vertical** dimension considers relations between models belonging to the same iteration in different activities (e.g. a design model realizing an analysis model). Two related models represent the same information, but from different abstraction level. Both related models also coexist and should be syntactically and semantically compatible with each other.

The **horizontal** dimension considers relations between artifacts belonging to the same activity in different iterations (e.g. a use case is extended by another use case). In this dimension new models are built or derived from previous models by adding new information that were not considered before or by modifying previous information. New models replace previous models that is to say that old models do not exist any more, as a consequence, there is no compatibility problem between these models.



**Figure 1.** dimensions in the software development process

Figure 1 illustrates the three dimensions described above. It lists the classical activities – requirements, analysis, design, implementation and test – in the vertical axis and the sequence of iterations in the horizontal axis.

Figure 2 summarizes both differences and similarities between dimensions, respect to two related models A and B.

Relations between models should be formally defined since the lack of accuracy in their definition can cause problems, for example:

- Wrong model interpretations and discussion regarding the model meaning: the interpretation done by the user that reads the model may not coincide with the interpretation of the model creator.
- Inconsistency among the different models: if the relation existing among the different sub-models is not accurately specified, it is not possible to analyze whether its integration is consistent or not.

- Evolution conflicts: when a model is modified, unexpected behavior may occur in other models that depend on it.

At the present the Unified Modeling Language UML is considered the standard modeling language for object oriented software development process. The specification of UML constructs and their relationships (UML 1997) is semi-formal, i.e. certain parts of it are specified with well-defined languages while other parts are described informally in natural language. There is an important number of theoretical works giving a precise description of core concepts of UML and providing rules for analyzing their properties; see, for instance the works of Evans et al.(1998;1999), Kim and Carrington (1999), Back et al.(1999), Breu et al.(1997), Knapp (1999), Övergaard (1999, 2000), Pons and Baum. (2000), Cibrán et al.(2000), Reggio et al.(2000), Smith et al.(2000). These works improve precision of syntax and semantics of isolated UML models, without dealing with relationships between models.

Dimension	Information that is specified by each model	life time
Internal	A and B contains complementary information that should be compatible	A and B coexist
Vertical	A and B contains the same information but from different abstraction level	A and B coexist
Horizontal	B updates information of A	A is replaced by B

**Figure 2:** comparisson between dimensions

In addition, Övergaard and Palmkvist (1998, 2000), Petriu and Sun (2000), Sendall. and Strohmeier, (2000) and Whittle et al. (2000) focus on relationships between different UML models. Following this direction, we classify relations between models along three different dimensions, proposing a formal description of them. This paper reports an extension of the work described in (Pons et al., 2000).

## 2. Internal-dimension relations

Every model is made up from a number of related sub-models (or artifacts) that have to be semantically compatible obeying to several constraints between them.

The UML specification document (UML, 1997) defines the abstract syntax of UML by class diagrams and well-formedness rules expressed in the Object Constraint Language OCL (UML, 1997). Most of the well-formedness rules in that document are examples of constraints on internal-dimension relations. For example

- rule for ClassifierRole in page 2-104 in (UML, 1997) saying that the features of the ClassifierRole must be a subset of those of the base Classifier:

$\forall r: \text{ClassifierRole} \bullet$   
 $(r.\text{allAvailableFeatures} \subseteq r.\text{base.allFeatures})$

- rule for Association in page 2-42 in (UML, 1997) stating that the connected Classifiers of the AssociationEnds should be included in the Namespace of the Association:

$\forall a: \text{AssociationEnds} \bullet \forall r \in a.\text{allConnections} \bullet$   
 $(r.\text{type} \subseteq a.\text{nameSpace.allContents})$

After a number of revisions, the UML specification document still contains ambiguities and inconsistencies. We have been analyzing internal relationships between models in order to improve their specification. For example, a classifier role is a description of the features required in a particular collaboration, i.e. a classifier role is a projection of a classifier. The classifier so represented is referred to as the base classifier. Collaboration, classifier and classifier roles are generalizable elements. One possible way to specialize a collaboration is to specialize some classifier role in the collaboration. The UML specification document gives a set of OCL rules to restrict generalization relation between collaborations. The rule number 5 in page 2-106 in (UML, 1997) states that “a role with the same name as one of the roles in a parent of the Collaboration must be a child (a specialization) of that role”. This rule is expressed by the formula:

$\forall s: \text{Collaboration} \bullet \forall c \in s.\text{contents}$   
 $\bullet \forall p \in s.\text{parent.allContents} \bullet$   
 $(c.\text{name} = p.\text{name} \rightarrow p \in c.\text{allParents})$

This rule is too restrictive, since the specialization of a classifier role could be accomplished in other ways. To solve this problem the rule above can be extended in the following way:

$\forall s: \text{Collaboration} \bullet$   
 $\forall c \in s.\text{contents} \bullet \forall p \in s.\text{parent.allContents} \bullet$   
 $(c.\text{name} = p.\text{name} \rightarrow$   
 $(p \in c.\text{allParents} \vee (p.\text{allAvailableFeatures} \subseteq$   
 $c.\text{allAvailableFeatures} \wedge p.\text{base} \in c.\text{base.allParents})) )$

Other examples of improvements to UML, and inconsistencies that were detected can be read in [Cibran et al. 2000]:

On the other hand, within the internal-dimension we consider relationships between separated models defining different views of a system (e.g. Class diagrams specifying structural aspects and StateMachines describing behavioral aspects). Although each one of these models has its self-contained meaning, global compatibility rules among them should be preserved. The following ones are examples of compatibility rules; more detailed examples can be read in (Pons 1999).

Example 1: Pre/post conditions vs. State Machines

Any model element may be associated with a constraint that expresses some property of it. There are problems when the constrained element has also a behavior that is precisely defined elsewhere in the model. For example, a constraint on an operation (as a pre-post condition) may be inconsistent with the effects of the transitions triggered by its calls in the associated state machine. As a consequence, it is necessary to integrate both views of the system guaranteeing that they are consistent with each other.

Example 2: Generalizations vs. other elements

Generalization diagrams have a strong influence on other diagrams in the model of the system.

For example, if two classes  $c_1$  and  $c_2$  are connected by a generalization relation (e.g.  $c_1$  is a subclass of  $c_2$ ), the behavior of instances of  $c_1$  should be a refinement of the behavior of instances of  $c_2$ . This requirement is defined by the following formula:

$\forall c_1, c_2: \text{Classifier} \bullet (\text{IsA}(c_1, c_2) \rightarrow$   
 $\text{refinement}(\text{behavior}(c_1), \text{behavior}(c_2)))$

A similar problem occurs when constraints are linked to classes in a generalization hierarchy: if  $c_1$  is a subclass of  $c_2$  then all the constraints over  $c_1$  should be consistent with all the constraints on  $c_2$ . This requirement is expressed by the following formula:

$\forall c_1, c_2: \text{Classifier} \bullet (\text{IsA}(c_1, c_2) \rightarrow$   
 $\text{consistent}(\text{constraints}(c_1) \cup \text{constraints}(c_2)))$

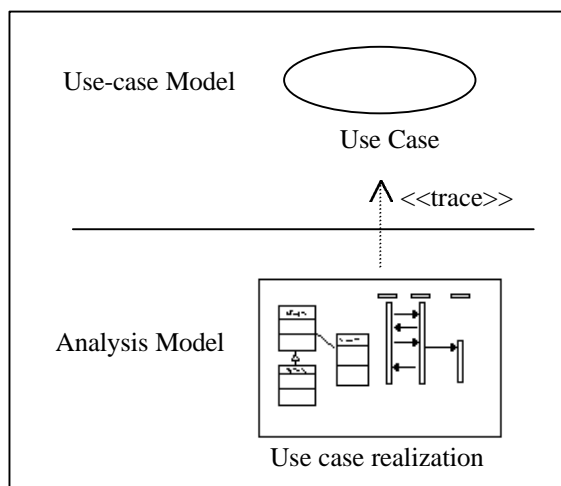
## 3. Vertical-dimension relations

In this section we analyze vertical relations, that is to say relations between models belonging to the

same iteration in different activities. Due to space limitations we only describe relationships between the requirement phase and the analysis phase.

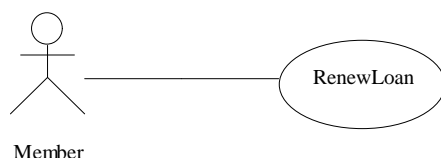
### 3.1. Creating analysis models from use cases

A use case in the use-case model is realized by a collaboration within the analysis model that describes how a use case is realized and performed in terms of analysis classes and their interacting analysis objects. A use case realization has class diagrams that depict its participating analysis classes, and interaction diagrams that depict the realization of a particular flow or scenario of the use case in terms of analysis object interactions. Figure 3 shows the relation between a use case and its realization.



**Figure 3:** relation between a use case realization in the analysis model and a use case in the use-case model.

**Example:** We present the model of a system to maintain a Library. The members of the library share a collection of books. The system should allow them to borrow books, to return them or to renovate a loan. When returning or when renovating the loan of a book, the member should pay a fee. In the event this fee is not paid, the member won't be able to borrow a new book or to



**Figure 4:** renewLoan use case

renovate a loan. Figure 4 shows the use case RenewLoan. This use case specifies the functionality of the system, for the renew of a loan.

Use cases can be specified in a number of ways. Generally natural language structured as a conversation between user and system is used, see (Jacobson et al., 1993). The conversation shows the request of a user and the corresponding answers of the system, at a high level of abstraction. Figure 5 shows a conversation between an actor (a member of the library) and the system. The conversation considers the normal action sequence and also alternative sequences (e.g. the case in that the book is not available).

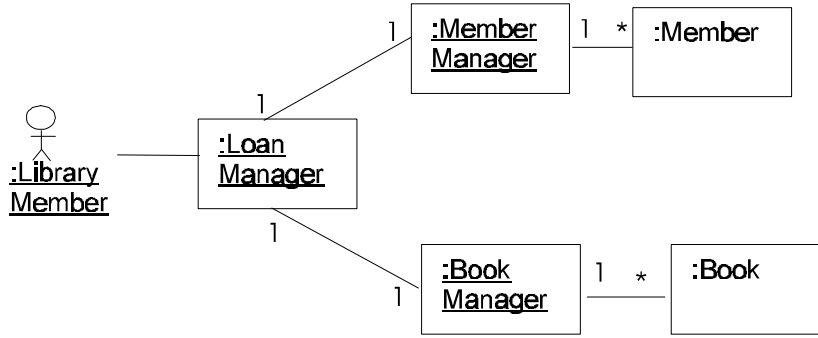
In the UML a UseCase is a kind of Classifier having a collection of operations (with its corresponding methods). Operations describe messages that instances of the use case can receive. Methods describe the implementation of operations in terms of action sequences that are executed by the instances of the use case. In general instead of having a set of operations, a use case has only a single operation, for example the RenewLoan use case has a single operation named “ask for renew loan”. The method that implements that operation contains the set of action sequences, some of the sequences in this set correspond to normal execution paths, while others correspond to alternative cases.

User Actions	System Answers
1. ask for renew loan	2. validate member id 3. validate book availability 4. ask for debt 5 renew loan
<u>Alternatives:</u>	
1. member identification is not valid -> reject loan	
2. book is not available -> reject loan	
3. member has debt -> ask for payment, then renew loan	

**Figure 5:** Use Case Conversation

Let uc be the use case defined above. The definition of uc (using the standard notation and metamodel of UML (in (UML, 1997) page 2-114) is as follows:

```
uc.operations = <op1>
op1.name=ask for renew loan
op1.method.body=
    {< validate member id, validate book availability,
ask for debt, renew loan>,
< validate member id, reject loan>,
< validate member id, validate book availability,
reject loan>,
```



**Figure 6.** Realization of the use case: collaborating ClassifierRoles

< validate member id, validate book availability,  
ask for debt, ask for payment, renew loan >}

In general we abbreviate `op.method.body` by `op.actionSequence`. The body of a method is a procedure expression specifying a possible implementation of an operation. The definition of procedure expressions is out of the scope of UML, here we interpret a procedure expression as a set of action sequences.

#### The realization of the use case:

Figure 6 shows a set of Classifier Roles and their connections, while figure 7 shows one of the iteration diagrams specifying the message flows between objects playing the roles in the collaboration. Figure 8 contains the textual representation of the diagrams. These diagrams are expected to realize the use case above; this fact will be formally proved in next section.

### 3.2. Formalizing the realization relation between Use Cases and Collaborations

Lets define a set of concepts that are necessary in order to formalize the relations between use cases and collaborations.

**Def. 1:** let  $(MS, \leq)$  be the poset of messages in an interaction (messages are partially ordered by the predecessor/successor relation). The set of linearizations on  $MS$  is defined as the set of sequences of messages in  $MS$  (i.e. the chains in the poset), and it is denoted as  $lin(MS, \leq)$ .

**Def. 2:**  $maxLin(MS, \leq)$  is the set of maximal linearizations on  $MS$ . It is obtained from  $lin(MS, \leq)$  by dropping every sequence that is contained in another sequence in the set, for example:

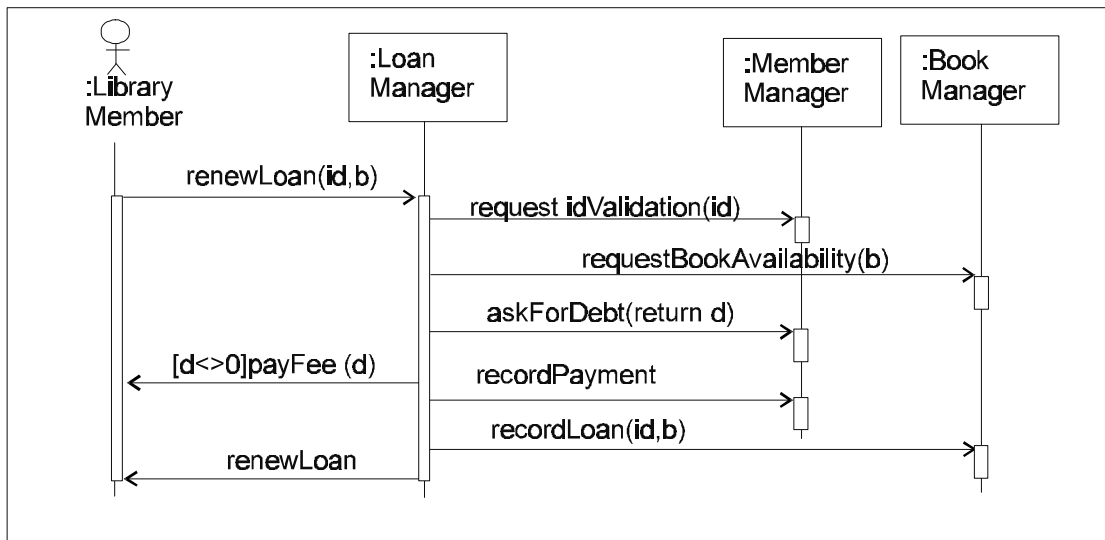
$lin(MS, \leq) = \{ \langle a, b, c, d \rangle, \langle b, c \rangle, \langle c, d \rangle \}$

$maxLin(MS, \leq) = \{ \langle a, b, c, d \rangle \}$

**Def. 3 :** let  $S$  be a set of sequences of actions.  $external(S)$  denotes the sequences of  $S$  obtained omitting all the actions that are not visible externally.

**Def. 4:** a *conformance declaration* is a correspondence between action names in a use case and action names in a collaboration. Each name in the use case is mapped to (a name of) an action in the collaboration. This mapping provides more flexibility in the development process allowing analysts to modify the name of the actions as the process evolves.

For example, the following is a *conformance declaration* between the Use Case and the



**Figure 7:** part of the Realization of the use case: one Interaction diagram

Collaboration above:

### Actions in the UC- Actions in the collaboration

ask for renew loan ---> renewLoan(id,b)  
 validate member id -->requestIdValidation(id)  
 validate book av. ----->requestBookAvailability(b)  
 ask for debt----->askForDebt(ret d)  
 ask for payment----->payFee(d)  
 renew loan -----> renewLoan  
 reject loan -----> reject

At this point we can define the *realization relation* between a Collaboration C and a Use Case UC. A Use Case is realized by a Collaboration if the Classifiers Roles in the Collaboration jointly cooperate to perform the behavior specified by the Use Case, but not more. In the case that the Collaboration includes more behavior than the one specified by the Use Case, the Use Case would be only a partial specification of the behavior described by the Collaboration. On the other hand, a use cases specifies actions that are visible from outside the system, but do not specify internal actions, such as creation and destruction of instances, communication between internal instances, etc. (for example, recordPayment and recordLoan are internal actions)

**Definition 5:** A collaboration C is a realization of a Use Case UC according to the conformance declaration  $\delta$ , denoted  $C \delta UC$ , if both of the following hold

a-  $\forall uo \in UC.operation. \forall ut \in uo.actionSequence. \exists int \in C.interaction. \exists ms \in lin(int.message).$

$\delta(uo.name) = act.operation.name$   
 $\wedge \delta^+(ut) = external((ms.tail).actions)$

b-  $\forall int \in C.interaction. \forall ms \in maxLin(int.message)$   
 $\cdot \exists uo \in UC.operation. \exists ut \in uo.actionSequence.$   
 $\delta(uo.name) = act.operation.name$   
 $\wedge \delta^+(ut) = external((ms \rightarrow tail).action)$

Where:

act = (ms.head).action  
 ms.head is the first element in the sequence ms  
 ms.tail is the subsequence obtained from ms by dropping the first element  
 ms.actions is an abbreviation for  
 ms.collect (e | e.action)  
 $\delta^+(ut) = ut.collect (a | \delta(a))$

Definition above states that every action sequence specified by the Use Case must have a corresponding action sequence in the Collaboration, that is equal to it (except for internal actions), and vice versa.

## 4. Horizontal-dimension relations

In this section we analyze horizontal relations, that is to say relations between models belonging to the same activity in different iterations.

### 4.1. Evolving the use-case model

A use case model may be evolved in different ways. The UML considers at least two forms of evolution: the *extends* and the *generalization* relationships between use cases. In this paper we only take into consideration the former.

The extend relation represents the enrichment of a use case by the definition of additional actions (see

Let RenewLoan be the Use Case defined above, and let CRenewLoan be the collaboration. The definition of CRenewLoan (using the standard notation and metamodel of UML (UML 99, page 2-100) is as follows:

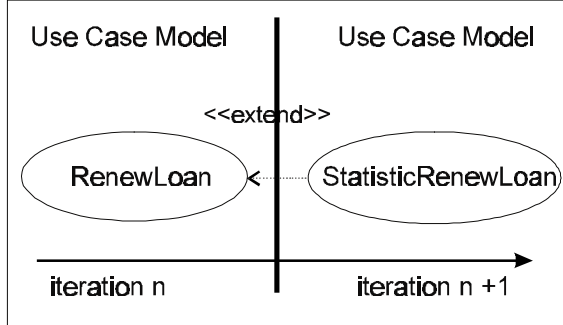
```
CRenewLoan.representedClassifier= RenewLoan
CRenewLoan.interaction={int1,int2, int3,int4}
CRenewLoan.classifierRole={R1,R2,R3,R4,R5}
R1.name=LoanManager, R2.name=Book, R3.name=Member,
R4.name=MemberManager, R5.name=BookManager
CRenewLoan.associationRole={A1,A2,A3,...} .....
int1.message={ (Actor, LoanManager, renewLoan(id,b)), (LoanManager, MemberManager, requestIdValidation(id)),
(LoanManager, BookManager, requestBookAvailability(b)), (LoanManager, MemberManager, askForDebt(d)),
( LoanManager, BookManager, renewLoan) }
int2.message={ (Actor, LoanManager, renewLoan(id,b)), (LoanManager, MemberManager, requestIdValidation(id)),
(LoanManager, BookManager, requestBookAvailability(b)), ( LoanManager, MemberManager, askForDebt(d)),
( LoanManager , Actor,payFee(d) ), ( LoanManager, BookManager, renewLoan) }
.....
```

Where each message m is represented by a triple (m.sender,m.receiver,m.action), where m.sender denotes the role of the instance that invokes the communication, m.receiver is the role of the instance that receives the communication, m.action is the action which causes a stimulus to be sent according to the message.

**Figure 8.** textual representation of the Collaboration

figure 9). An extend relationship from use case A to use case B indicates that an instance of use case B may include (constrained by specific conditions specified in the extension) the behavior specified by A.

The definition of extend includes both a condition



**Figure 9:** relation between a use case in the use case model and its extension

for the extension and a reference to an extension point in the target use case, that is, a position in the use case where additions may be made. Once an instance of a (target) use case reaches an extension point to which an extend relationship is referring, the condition of the relationship is evaluated. If the condition is fulfilled, the sequence obeyed by the use-case instance is extended to include the sequence of the extending use case.

#### Example:

The use case in figures 4 and 5 can be extended in order to count how many people have renovated the loan of a technical book. This extension can be achieved without modifying the original use case, by means of an extend relationship and a new use case specifying the increment of behavior. Figure 9 shows this relationship between use cases. In this case the extension point specified by the extend relationships is the action of renewing a loan. The condition of the extension is that the book is a technical one.

Let Statistic be the use case above mentioned specifying the increment of behavior. Statistic has a single operation with a single action sequence, as follows:

```
Statistic.operation.actionSequence=
{<updateRenewsCounter>}
```

The extend relationship *ext* is as follows:

```
ext.base= RenewLoan
ext.extension= Statistic
ext.condition= the book is technical
ext.extensionPoint= { renew loan }
```

Let StatisticRenewLoan be the use case that developers expect to obtain from RenewLoan by the application of the extension above, i.e.

StatisticRenewLoan = RenewLoan  $\oplus_{\text{ext}}$  Statistic (operation  $\oplus_{\text{ext}}$  between use cases is formally defined in next section).

The textual representation of the expected use case is as follows:

```
StatisticRenewLoan.operation.actionSequence=
{< validate member id, validate book availability,
ask for debt, renew loan, updateRenewsCounter> ,
< validate member id, reject loan>,
< validate member id, validate book availability,
reject loan>,
< validate member id, validate book availability,
ask for debt, ask for payment, renew loan ,
updateRenewsCounter >}
```

#### Formalizing use case extensions:

A use Case UC is the extension of UC1 by UC2 through an “extend” relationship *ext*;

i.e.  $UC = UC1 \oplus_{\text{ext}} UC2$  if the following holds:

**a- Applicability Conditions:** UC1 is extensible by *ext* if for each extension point of *ext*, there exist a corresponding action inside the sequences of actions of the use case:

$$\forall i \in \text{ext.extensionPoint}. \exists uo \in UC1.operation . \\ \exists uo \in uo.actionSequence . i.location \in uot$$

**b- UC1-Completeness:** every action sequences in UC1 is extended in every possible way:

$$\forall o1 \in UC1.operation . \exists o \in UC.operation . \\ ( o.name=o1.name \wedge (\forall s1 \in o1.actionSequence . \\ \text{extensions}(s1,\text{ext},UC2) \subseteq o.actionSequence) )$$

**c- UC1-Correctness:** every action sequence in UC is an extension of some action sequence in UC1.

$$\forall o \in UC.operation . \exists o1 \in UC1.operation . \\ (o.name=o1.name \wedge (\forall s \in o.actionSequence . \exists s1 \in o1 . \\ \text{actionSequence} . s \in \text{extensions}(s1,\text{ext},UC2) ) )$$

#### Definition 6 (function definitions):

*isExtensible*: ActionSequence x Extend

The predicate is true if the action sequence contains some extension point defined by the extend relation.

$$\forall s: \text{ActionSequence} . \forall \text{ext}: \text{Extend} . \\ \text{isExtensible}(s,\text{ext}) \leftrightarrow \exists i \in \text{ext.extensionPoint} . \\ i.location \in s$$

*extensions*: ActionSequence x Extend x UseCase -> Set(ActionSequence)

The function  $extensions(s, ext, uc)$  returns the set of all possible extensions of the sequence  $s$  given by the Extend relation  $ext$  and the Use Case  $uc$ . The function is defined by cases.

Case 1:  $\neg isExtensible(s, ext)$   
 $extensions(s, ext, uc) = \{s\}$

Case 2:  $isExtensible(s, ext)$   
 $extensions(s, ext, uc) =$   
 $\{ before(s, i.location); s2; after(s, i.location) /$   
 $i \in ext.extensionPoint \wedge i.location \in s \wedge$   
 $s2 \in uc.actionSequence \}$

**Definition 7:** UC extends UC1 if there exists a use case UC2 such that UC is the extension of UC1 by UC2 through an ext relation:

$$UC \text{ extends}_{ext} UC1 \leftrightarrow \exists UC2. (UC = UC1 \oplus_{ext} UC2)$$

## 4.2. Evolving the collaboration model

The UML does not consider special dependency relationships between Collaboration. However since Collaborations realize Use Cases, it is important to reflect the relationships between Use Cases (e.g. extend relationships) on its realizing Collaborations. As well as Use Cases are extended by adding actions (defined in other Use Case), Collaborations can be extended with additional message sequences specified in another Collaboration.

For further details about the extension relationship between Collaborations based on the corresponding extension relationship between Use Cases, readers are referred to (Giandini et al., 2000).

## 5. Relations between relations

As well as the different models of a system are not independent, the different relationships among models neither are independent. In this section we point out some properties of relationships.

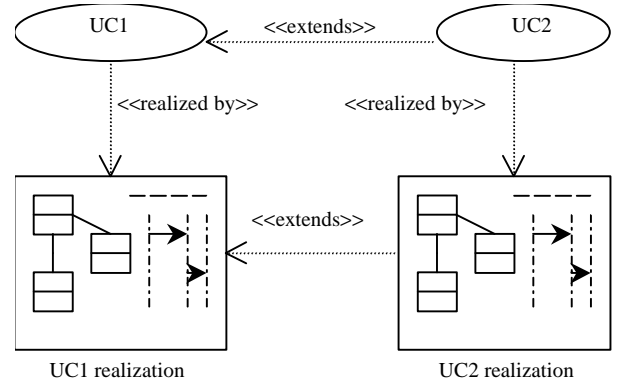
**Theorem:** Let UC1 and UC2 be use cases. If UC2 is an extension of UC1 through  $ext$ , and each use case is realized by a corresponding collaboration, then there exists a collaboration realizing UC2 such that it is an extension of C1:

$$\forall UC1, UC2: UseCases. \forall C1, C2: Collaborations .$$

$$(( UC2 \text{ extends}_{ext} UC1 \wedge C1 \text{ realizes } UC1 \wedge C2 \text{ realizes } UC2 )$$

$$\rightarrow \exists C3. (C3 \text{ extends}_{ext} C1 \wedge C3 \text{ realizes } UC2))$$

Figure 10 illustrates the relation between the extend relationship and the realization relationship.



**Figure 10:** relations between relations in the Unified Process

## 6. Concluding Remarks

During the Unified Process, a variety of models of the system is developed. All these models are not independent, but they are related to each other. Elements in one model have trace dependencies to other models; they are semantically overlapping and together represent the system as a whole.

Relations between models should be formally defined since the lack of accuracy in their definition can lead to wrong model interpretations, inconsistency among models, inconsistent evolution of models, etc.

In this paper we classify relations between models along three different dimensions (i.e. artifact dimension, activity dimension and iteration dimension), proposing a formal description of them. The goal of the proposed formalization is to provide formal foundations for tools that perform intelligent operation on models, such as:

- checking the consistency between models belonging to different activity, such as a requirements model and an analysis model (i.e. consistency along the activity dimension).
- checking the consistency of models through its evolution along the process (i.e. consistency along the iteration dimension)
- checking the internal consistency of models (i.e. consistency along the artifact dimension).
- checking the consistency of the process as a whole (i.e. consistency among the different dimension).

A step beyond this work will be to use the formalization to define automatic rules of evolution that assist the software engineer during the development process. For example, given an analysis model the rules could suggest possible forms of realizing such a model in terms of design models, and given a model the rules could suggest possible way to refine or to extend it.



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